

# Mathematics Support Capsules

## WORD PROBLEMS IN ALGEBRA

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1. A Cornell student walked six miles to class and was  $\frac{1}{4}$  hour late. If he had walked two miles per hour faster he would have been on time. What was his original speed?
2. A motorist drove 280 miles. If he had gone 5 m.p.h. faster he could have made his trip in 1 hr. less time, how fast did he drive?
3. If  $1\frac{1}{2}$  chickens lay  $1\frac{1}{2}$  eggs in  $1\frac{1}{2}$  days, how many eggs do 6 chickens lay in 7 days?
4. A bridge looks like the graph of  $y = -3x^2 + 12x + 8$ . You have a 10 ft. high truck with a load 8 ft. wide. Can you make it under the bridge?
5. A bamboo 18 ft. high was broken by the wind. Its top bent over and touched the ground 6 ft. from the root. At what point along the length of the bamboo did the break occur?
6. Diophantus lived  $\frac{1}{6}$  of his life in childhood,  $\frac{1}{12}$  in youth,  $\frac{1}{7}$  more as a bachelor. 5 years after his marriage was born a son who died 4 years before his father, at half his father's final age. How old was Diophantus when he died? How old was his son when his son died?
7. At noon, a bus leaves Boston and travels due north at 40 m.p.h. At 2:00 p.m. a train leaves Boston and travels due west at 60 m.p.h. When are the bus and the train 200 miles apart?

Conclusion:

$$d = rt \rightarrow 6 = r(t + \frac{1}{4})$$

$$\rightarrow 6 = (r+2)(t)$$

$t =$  time necessary to be on time =  $\frac{3}{4}$  hour  
 $r =$  original rate =  $6$  mph

2 eqns. with 2 unknowns:

solve first for  $r$  in terms of  $t$ , then substitute for  $r$  in second to get an equation for  $t$  alone.

$$r = \frac{6}{t + \frac{1}{4}} \Rightarrow 6 = (\frac{6}{t + \frac{1}{4}} + 2)t \Rightarrow \text{(multiply out)} \quad t = -1 \text{ or } t = \frac{3}{4}$$

no help in this problem

then when you have  $t$  you can find  $r = \frac{6}{t + \frac{1}{4}}$

?  $d = rt \rightarrow 280 = vt$   
 $\rightarrow 280 = (v+5)(t-1) \rightarrow t = 8, v = 35$

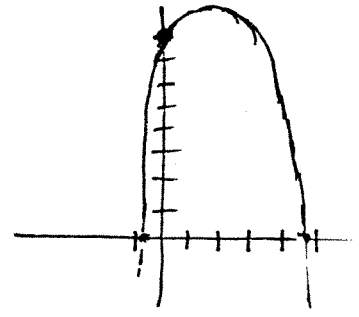
? if  $1\frac{1}{2}$  hens lay  $1\frac{1}{2}$  eggs in  $1\frac{1}{2}$  days  
 then  $1\frac{1}{2}$  hens lay 1 eggs in 1 day  
 $1\frac{1}{2}$  hens lay 7 eggs in 7 days  
 $\frac{6}{1\frac{1}{2} \times 4}$  hens lay  $\frac{7 \times 4}{28}$  eggs in 7 days

This is just one of many ways to do this - its important to note that all 3 quantities do not change together

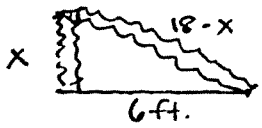
Graph the curve,  $y = -3x^2 + 12x + 8$ , which is a parabola:

x	y
0	8
4	0
-2	0

x-intercepts, by quadratic formula  
 $\frac{-12 \pm \sqrt{144 + 96}}{-6} \approx 4\frac{2}{3}, -\frac{2}{3}$



and just these 2 points are not spaced widely enough for the truck to pass between.

?  by Pythagorean Theorem,  $(18-x)^2 = x^2 + 6^2 \Rightarrow x = 8 \text{ ft.}$

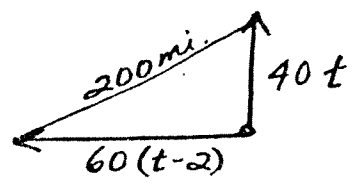
Let  $x =$  Diophantus' age at death. Then

$$\frac{x}{6} + \frac{x}{12} + \frac{x}{7} + 5 + \frac{x}{2} + 4 = x$$

childhood + youth + bachelor + married + son + years survived son. = lifetime

and  $x = 84 \text{ yrs.}$

7.



Pythagorean Theorem, again.

$$200^2 = (40t)^2 + 60(t-2)^2$$

solution:  $t = 4 \text{ hours} = 4:00 \text{ PM}$

$t =$  time after noon